## Any excaling of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice. Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.

## Fourth Semester B.E. Degree Examination, Dec.2014/Jan.2015 Engineering Mathematics – IV

Time: 3 hrs.

Max. Marks: 100

Note: 1. Answer any FIVE full questions, selecting atleast TWO questions from each part.
2. Use of statistical table is permitted.

PART – A

- 1 a. Employ Taylor's series method to find an approximate solution to find at x = 0.1 given  $\frac{dy}{dx} = x^2$ , y(0) = 1 by considering upto fourth degree term. (06 Marks)
  - b. Solve the following by Euler's modified method  $\frac{dy}{dx} = \log(x + y)$ , y(0) = 2 to find y(0.4) by taking h = 0.2. (07 Marks)
  - c. Given  $\frac{dy}{dx} = x^2$  (Hy) and y(1) = 1, y(1.1) = 1.233, y(2) = 1.548, y(1.3) = 1.979. Evaluate y(1.4) by Adams-Bash forth withod. Apply corrector formula twice. (07 Marks)
- 2 a. Solve  $\frac{dy}{dx} = 1 + xz$  and  $\frac{dz}{dx} = -xx$  or x = 0.3 by applying Runge Kutta method given y(0) = 0 and z(0) = 1. Take h = 0.3.

  (06 Marks)

  b. Use Picard's method to obtain the second approximation to the solution of
  - $\frac{d^2y}{dx^2} x^3 \frac{dy}{dx} x^3y = 0 \quad \text{give } y(0) = 1, \ y'(0) = 0$  Also find y(0.1). (07 Marks)
  - c. Apply Milne's method to compute y(0.4) given y'' + y + y = 0, y(0) = 1, y'(0) = 0, y(0.1) = 0.995, y'(0.1) = -0.0995, y(0.2) = 0.9802, y'(0.2) = -0.196, y(0.3) = 0.956 and y'(0.3) = -0.286. (07 Marks)
- 3 a. Derive Carrell Riemann equation in Cartesian form.

(06 Marks)

b. Find an analytic function f(z) whose real part is  $\frac{\sin 2x}{\cosh 2y - \cos 2x}$  and hence find its imaginary part.

If f(z) is a holomorphic function of z, then show that  $\left\{\frac{\partial}{\partial x}|f(z)|\right\}^2 + \left\{\frac{\partial}{\partial y}|f(z)|\right\}^2 = |f(z)|^2$ .

4 a. Discuss the transformation  $w = z + \frac{1}{z}$ .

(06 Mark

b. Find the BLT which maps the points z = 1, i, -1 to w = i, 0, -i. Find image of |z| < 1.

(07 Marks)

c. Evaluate  $\int_{C} \left\{ \frac{\sin \pi z^2 + \cos \pi z^2}{(z-1)^2 (z-2)} \right\} dz \text{ where 'C' is circle } |z| = 3.$  (07 Marks)

- (06 Marks)
- (07 Marks)
  - Derive Rodrique's formula  $P_n(x) = \frac{1}{2^n |n|} \frac{d}{dx^n} [(x^2 1)^x].$ (07 Marks)
  - State the axioms of probability. For any two events A and B, prove that,  $P(A \cup B) = P(A) + P(B) - P(A \cap B).$

A box 'A' contains 2 white and 4 black balls. Another box 'B' contains 5 white and 7 black balls. A ball is transferred from the box A to the box B. Then a ball is drawn from the box B. **Kind** the probability that it is white. (07 Marks)

c. In a sertain college 4% of the boys and 1% of girls are taller than 1.8m Further more 60% of the tradents are girls. If a student is selected at random and is found to be taller than 1.8m, what is the probability that the student is a girl? (07 Marks)

- probables density of a continuous 7 given  $p(x) = y_0 e^{-|x|}, -10$   $\infty$ . Find  $y_0$ . Also find the mean. (06 Marks)
  - b. Obtain the mean and variance of binomial distributions

(07 Marks) c. In a test on 2000 electric balbs, it was found that the life of a particular make was normally distributed with an average the of 2040 hours and SD of 60 hours. Estimate the number of bulbs likely to burn for.

- i) More than 2150 hours.
- ii) Less than 1950 hours.
- More than 1920 hours but less th Given A(1.5) = 0.4332,  $A(1.83) \le 0.3664$ , A(2) = 0.4772.

(07 Marks)

- In a city 'A' 20% of a random sample of 900 Chool boys had a certain slight physical 8 defect. In another city B 8.5% of a random sample of 1600 school boys had the same defect. Is the difference between the proportions is significant? Why?
  - b. A manufacturer claimed that atleast 95% of the equipment which he supplied to a factory conformed to specifications. An examination of a sample of 200 pieces of equipment revealed that 18 of them were faulty. Test his claim at a significance level of 1% and 5%. (07 Marks)

No. of heads 0 1 2 3 4

Frequency 6 27 72 112 71

Test the hypothesis that the data follow a binomial distribution